

Exercise-set 1. Solutions

1. a) $26^5 - 26$,
 b) $7!/(2! \cdot 3!)$,
 c) $\binom{29}{5}$,
 d) $5 \cdot 25 \cdot 24 \cdot 23 \cdot 22$,
 e) $\binom{25}{4} = \binom{26}{5} - \binom{25}{5}$,
 f) $26^5 - 25^5$,
 g) $\binom{25}{5} + \binom{24}{4}$,
 h) $\binom{26}{9}$,
 i) $\sum_{k=0}^{26} \binom{26}{k} = 2^{26}$.
2. a) 5^{25} ,
 b) $\binom{24}{20}$.
3. a) $\binom{30}{6}$,
 b) $\binom{35}{6}$,
 c) $\binom{100}{4}$.
4. $\binom{30}{4}^{16}$.
5. a) $\binom{90}{20}$,
 b) $\binom{90}{20} + 19$,
 c) $\binom{89}{4} \cdot \binom{89}{13}$,
 d) $\binom{89}{5} + \binom{88}{3}$.
6. $\binom{26}{4}$.
7. a) $\binom{20}{4} \cdot ((\binom{20}{4} - 1) \cdot ((\binom{20}{4} - 2))$.
 b) $\binom{20}{4} \cdot ((\binom{20}{4} - 1) \cdot ((\binom{20}{4} - 2) - \binom{19}{4} \cdot ((\binom{19}{4} - 1) \cdot ((\binom{19}{4} - 2))$.
 c) $3 \cdot \binom{19}{3} \cdot \binom{19}{4} \cdot ((\binom{19}{4} - 1))$.
8. $26 \cdot 25 \cdot 24 \cdot 23 \cdot 4^5$.
9. $6 \cdot \binom{5}{3} \cdot 11!/(3! \cdot (2!)^3)$.
10. $\binom{15}{3} \cdot \binom{12}{4} \cdot 2^4$.
11. $\binom{12}{4} \cdot \binom{8}{3} \cdot 24^5$.
12. $\binom{5}{5} \cdot \binom{5}{0} + \binom{5}{4} \cdot \binom{5}{1} + \binom{5}{3} \cdot \binom{5}{2} = \binom{10}{5}/2$.
13. $26^6 + \binom{6}{1} \cdot 26^5 \cdot 10 + \binom{6}{2} \cdot 26^4 \cdot 10^2$.
14. $\binom{6}{3} \cdot 26^3 \cdot 10^3 - 4 \cdot 26 \cdot 10^3$.
15. $1 \cdot \binom{6}{2} \cdot 9^4 + 8 \cdot \binom{6}{3} \cdot 9^3$
16. a), b) The numbers of even and odd subsets are equal (see ex. 19/a).
17. 2^{100} .
18. a) 100,
 b) 100
 c) 36.
19. a) 0,
 b) $\binom{100}{10}$.